## SECTION 1

## Whole Numbers

## Unit 1. Basic Principles of Whole Numbers

Unit 2. Adding Whole Numbers
Unit 3. Subtracting Whole Numbers
Unit 4. Multiplying Whole Numbers
Unit 5. Dividing Whole Numbers

## Key Terms

addition borrowing carrying decimal number system denominate number difference digits dividend division
division sign ( $\div$ ) divisor
equals sign (=)
minus sign (-)
multiplication
multiplication sign ( $\times$ )
place value
plus sign (+)
product
quotient remainder rounding square subtraction sum whole number

## UNIT 1

## Basic Principles of Whole Numbers

## Objectives

After studying this unit, you will be able to:

- Identify the place value of whole numbers.
- Round whole numbers to a given place value.
- Recognize denominate numbers.

Carpenters and other workers in the building construction trades must develop a mastery of mathematics principles, operations, and formulas. Every aspect of the construction industry requires an understanding and accurate use of mathematical concepts. As a carpenter, you will need to be skilled in tasks such as reading a tape measure, estimating materials, and calculating rafter line length, just to name a few. Calculators can be an efficient tool when performing math operations, but they are not always available, or practical, on a construction site. Because of this, it is essential that carpenters learn basic math principles and develop the ability to solve operations without the use of a calculator.

## Place Values

The decimal number system, also known as the Arabic number system, uses 10 as its base unit. This system consists of 10 different digits: $0,1,2,3,4,5,6,7,8$, and 9 . Digits are symbols that are used to create everyday numbers.

Numerical values are expressed by placing a combination of digits together to create a whole number. A whole number is a numeral that stands alone as a unit and can contain multiple digits. Whole numbers do not include a fraction or a decimal. In the decimal number system, the value of the digit is determined by its location in the whole number. This value is called the place value. The following chart shows the place value of each digit within the number 5,694.


Add the values of each digit to determine the value of the whole number.

The digit 5 is in the thousands column
The digit 6 is in the hundreds column
The digit 9 is in the tens column
The digit 4 is in the ones column

$$
\begin{aligned}
5 \times 1,000 & =5,000 \\
6 \times 100 & =600 \\
9 \times 10 & =90 \\
4 \times 1 & =\underline{+4} \\
& =5,694
\end{aligned}
$$

## Math Tip

To make numbers easier to read, a comma is inserted after every third digit counting from the right.

## Example 1-1

What are the place values of the digits in the number 5,298,347?


## Example 1-2

Sometimes a zero is one of the digits within a whole number. Regardless of where it is located in the number, its place value remains zero.

What is the place value of the zero in the whole number 2,084 ?
The zero is in the hundreds column, so then $0 \times 100=0$.
The whole number would be read as two thousand eighty-four.

## Rounding Whole Numbers

There are times when whole numbers do not need to be exact. When calculating material estimates for a project or cost estimates for a quote, numbers can be rounded to a specific place value. Rounding numbers is the process of increasing or decreasing the value of the number to a specific place value. When calculating the area of the roof in the following image, the $1,382 \mathrm{sq} \mathrm{ft}$ roof would be rounded to $1,400 \mathrm{sq} \mathrm{ft}$ for estimating or purchasing the material. Because shingles are sold by the square ( 100 sq ft ), the area of the roof is rounded up to the next full square.


When calculating material estimates for a project, numbers are generally rounded up to account for how materials are sold or for waste factor. Other times, numbers can be rounded up or down to a specific place value depending on the situation.

## Steps for Rounding to a Nearest Place Value

1. Identify the place value to which the number is being rounded.
2. Identify the digit to the right of that place value.
3. If the digit to the right is 5 or greater, increase the place value number up by one (round up). If the digit to the right is 4 or less, do not change the place value number.
4. Change the remaining digits to the right to zeros.

## Example 1-3

Round the number 34,673 to the thousands place value.
The number in the thousands place value is 4 .

The digit to the right of the 4 is 6 .

Since 6 is greater than 5 , the 4 is rounded up by one, making it 5 . The remaining numbers to the right are changed to zero.

## Example 1-4

Round the number 16,841 to the hundreds place value.
The number in the hundreds place value is 8 .
16,841
The digit to the right of the 8 is 4 .
16,841
Since the 4 is less than 5 , the 8 is not changed but the remaining numbers to the right are changed to zero.

16,800

## Denominate Numbers

When working in construction, numbers will often be associated with a unit of measurement. Numbers consisting of a numeric value and a unit of measure are referred to as denominate numbers. Carpenters work with denominate numbers in every phase of the construction process from site prep to framing to final finish. For example, $32^{\prime}$ and $64^{\prime}$ are denominate numbers because they include a value ( 32 and 64 ) and a unit of measure (feet). Other examples include:

- 15 lb
- 64 sq ft
- 3 hours, 14 minutes, 45 seconds
- 2 tons, 600 pounds


## Carpentry Notes

## Paint Estimation

During the finishing stages of construction, carpenters take room measurements and purchase the appropriate quantity of paint for the walls and ceilings. This is one occasion when carpenters take exact calculations, and then round the number up. Rounding up will help cover any extra paint needed for touch-ups or mistakes. If 1 gallon of paint will cover an area of 400 sq ft , how many gallons of paint are needed for a 764 sq ft room?

To round up 764 sq ft to the nearest hundreds, look at the number to the right of the hundreds place value. As 6 is greater than 5 , then round up the hundreds place value to 8 , which gives you 800 sq ft . Since 1 gallon of paint will cover an area of 400 sq ft , 2 gallons of paint are needed for this project.

## Work Space/Notes

## Unit 1 Review

Name $\qquad$ Date
Class $\qquad$

Use the number 4,784,523 to answer the following questions.

1. Which digit is in the hundreds place?
2. Which digit is in the ten thousands place?
3. Which digit is in the tens place?
4. Which digit is in the hundred thousands place?
5. Which digit is in the thousands place?
$\qquad$

Use the number 4,721,593 to answer the following questions.
6. In which place value is the 3 ?
7. In which place value is the 7 ?
8. In which place value is the 4 ?
9. In which place value is the 9 ?
10. In which place value is the 1 ?


Round the following whole numbers to the indicated place value.
11. Round 172,839 to the ten thousands place value.
12. Round 74,613 to the thousands place value.
13. Round 93,827 to the tens place value.
14. Round $17,464,594$ to the millions place value.
15. Round 8,462 to the hundreds place value.
16. Round 729,381 to the hundred thousands place value.
17. Round 943 to the hundreds place value.
18. Round 91,735 to the tens place value.
19. Round $31,723,468$ to the ten thousands place value.
20. Round $6,527,914$ to the thousands place value.

Identify the denominate numbers in the following problems.
*See Appendix A
21. A carpenter cuts 64 boards to a length of $93^{\prime \prime}$ for wall studs*.
22. The floor plan called for 8 floor joists* to be installed $16^{\prime \prime}$ on center.
23. The dimensions on the floor plan are $16^{\prime}$ by $14^{\prime}$ for the 2 bedrooms.
24. The estimated time for 4 workers to shingle the roof was 6 hours, 30 minutes.
25. The 7-acre property building site will have 3 buildings on the north end.

